

An Approach for Community Cutting^{*}

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Abstract. Informational networks and networks created based on social interactions possess high complexity. Yet the networks can be decoupled into sets of vertices, communities, more interconnected among each other than by other vertices of the network. For mining internal structure of informational and social networks approach for finding community around a seed of vertices is described. Most of existing clustering approaches intend to identify all communities in the network, our goal is to identify the community around a vertex or a set of vertices. We give also short overview of tools for network analysis and their functionalities is given.

1 Introduction

Massive networks can be observed from various aspects of the world. Nowadays more massive networks have measurable and analysable form: informational networks such as the Web, networks of social interactions as phone call, SMS or email communication can be captured. We give overview of operations, representations and tools for modelling graphs. The intention is to build a basis for further development of a software tool for analysing massive graphs. We also introduce an approach for finding community around a set of vertices, which should perform better than other approaches mining all communities in the network.

Those networks that are interesting for research usually perform huge number of vertices and edges. The amount of data forces us to think about how to tackle spatial and computational complexity. Often the data does not fit in the system memory. Just for a glance: the crawls of a search engine has to process around 200 million web pages and 2 billion hyperlinks [4, page 10], the number of communications in a phone network can scale as 50 million for a month. Scalability is perhaps the most obvious problem spot one can notice when implementing and testing a tool for network analysis.

^{*} This work has been partially supported by the Scientific Grant Agency of the Ministry of Education of Slovak Republic grant No. VG1/ 0162/03, and by Science and Technology Assistance Agency under the contract No. APVT-20-007104.

2 Network Analysis Tools

Projects for massive network analysis and visualisation are being developed (Pajek [1], JUNG, InFlow, DyNet, Cyram NetMiner). These tools mostly provide functions such as ranking vertices according to their importance, centrality measurements, clustering and visualisation of the network and other functionalities.

We consider network representations as list of vectors: for every vertex a list of its neighbour vertices is defined; matrix representation: the adjacency matrix serves a good representation as useful operations can be performed on the adjacency matrix (computing co-citation matrix, importance ranking algorithms, like PageRank, HITS). However as most of networks being analysed are sparse, storing network as a matrix can cause too expensive space consumption. We find external storage of the network to a relational database as the simplest and most effective solution currently. Edges are defined as relations, containing edge head, tail and edge attributes.

The initial networks are usually objects for manipulations. These network manipulations result in changed networks, which are further analysed and should serve a basis for making decisions for the user or should present a list of results which helps navigation in the network. The following list of operations were chosen as the most interesting from our point of view.

Clustering Identification of clusters/community structures in the network. The input of the clustering operation is a graph and generates a list of clusters containing vertices, and a hierarchy of clusters.

Shrinking Shrinking sets of vertices to one vertex, for instance shrinking identified clusters to vertices.

Filtering Operations for filtering out edges and vertices with given criteria.

Co-citation network Operation over the adjacency matrix: $\mathbf{E}^T \mathbf{E}$.

Ranking Implementation of vertex/edge importance ranking, such as centrality measurements [2], PageRank [6] or HITS [3]

These operations generate a new network from the original one. We distinguish two modes for this process. In *generate-mode* a new graph is produced, which is completely independent of the originally processed. Generation of a graph from the source graph causes computational effort when it is executed, but every operation is done on the produced graph afterwards. For *wrap-mode* the graph manipulation decorates the graph under processing, every operation on the wrapper graph delegated to the data of the wrapped graph and does not create physically any graph. The produced graph is kind of a view of the processed graph. This mode causes small effort when it is executed, but a little more computation when the wrapper graph is processed. Also the spatial demands of this operation should be much smaller, as no graph is generated.

Shrinking, clustering and generation of cluster hierarchy are operations of *global decomposition*. *Local decompositions* are cutting out a part of the graph (for instance vertices of a component) or shrinking all but one cluster produces a context of the left alone cluster. Fig. 1 shows an illustration of the decompositions.

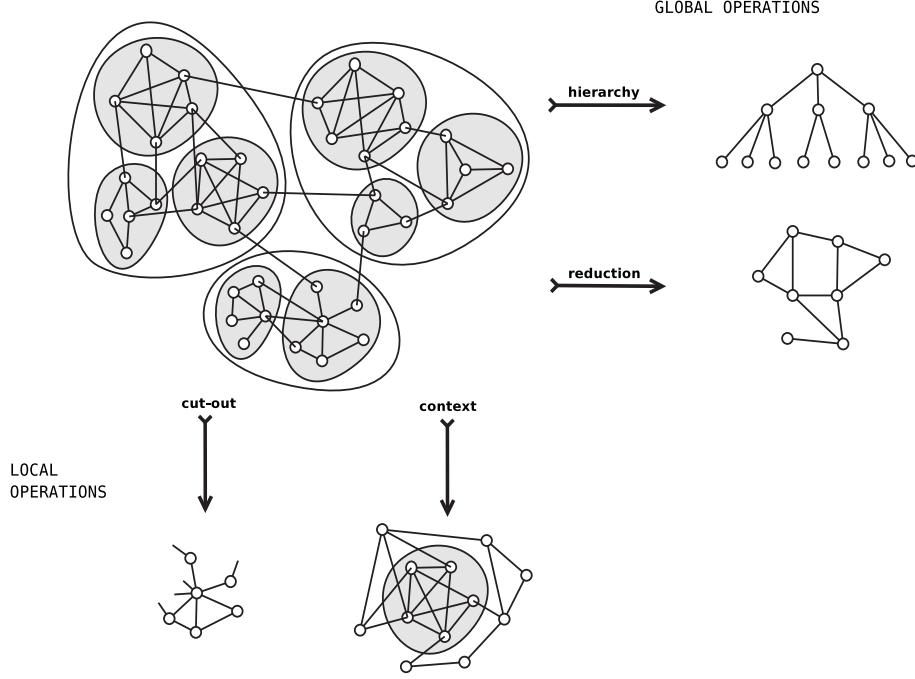


Fig. 1. Illustration of transforming graphs to other forms.

Clustering massive networks, consisting of even more million vertices can show up as too complex problem to solve. For instance Newman-Girvan edge-removal algorithm takes $O(mn^2)$ [5], other algorithms based on hierarchical performing worse separation of communities need $O(n^2)$ time for computation in case of sparse graph. Even this may be unfeasible for networks with more million vertices.

3 A community-cutting approach

We propose an algorithm for finding community containing an initial seed of vertices. As our intention is not to classify all vertices to communities, we need to traverse a smaller part of the network. We call this approach as community-cutting.

Our approach is a modified breath-first search algorithm (alg. 1). Whereas the BFS prioritises the vertices based on the distance from the seed vertices, varying priorities set as the proportion of the number of neighbours already cut-out and the total number of adjacent vertices are used.

The priorities are updated based of eq.1:

$$priority = \frac{|N_k \cap C|}{|N_k|} \quad (1)$$

where N_k is the number of neighbours of vertex k and C is the of vertices assigned to the community.

Algorithm 1: Community-cutting algorithm

Data: graph $G(V, E)$, seed of initial vertices S , maximum number of vertices to cut L

Result: set of cut-out vertices C

```

1  $C = S$ ;
2  $list = S$ ;
3 while  $list$  is not empty and  $|C| < L$  do
4    $v = pop(list)$ ;
5   add  $v$  to  $C$ ;
6   forall neighbours  $k$  of  $v$  do
7     if  $k$  not in  $C$  then
8       if  $k$  in  $list$  then
9         re-rank  $k$  in  $list$  with priority:  $\frac{|N_k \cap C|}{|N_k|}$ ;
10      else
11        add  $k$  to  $list$  with priority:  $\frac{1}{|N_k|}$ ;
12 return  $C$ ;
```

Algorithm traversing through the whole network visits $O(n + m)$ vertices and edges. Visiting a new vertex takes $O(\log n)$ time for updating the priority using Fibonacci-heap in the worst case. Therefore the whole algorithm takes generally $O(m + n \log n)$ time.

We used a network of mobile communications of one month period acquired from a mobile operator. The analysed data set is not a public collection. The communication consisted of more types including calls, SMS, FAX, GPRS and MMS. This is a huge network of more than 57 million edges, well capturing social interactions. We considered the network as oriented. During the testing problem with vertices of very high degree (higher than 100.000) was noticed. For tackling the problem vertices with degree higher than 1000 were filter out and not visited during the community cutting.

Fig.2 shows the priorities of vertices assigned to the community during running of alg.1. Priority of a vertex gives what proportion of its incoming neighbours is already assigned to the community and the total number of incoming edges. If the priorities are low, perhaps the algorithm reached the borders of a cluster of vertices and it is approaching to a neighbour cluster. Fig.2 shows a wavering evolution of the priorities.

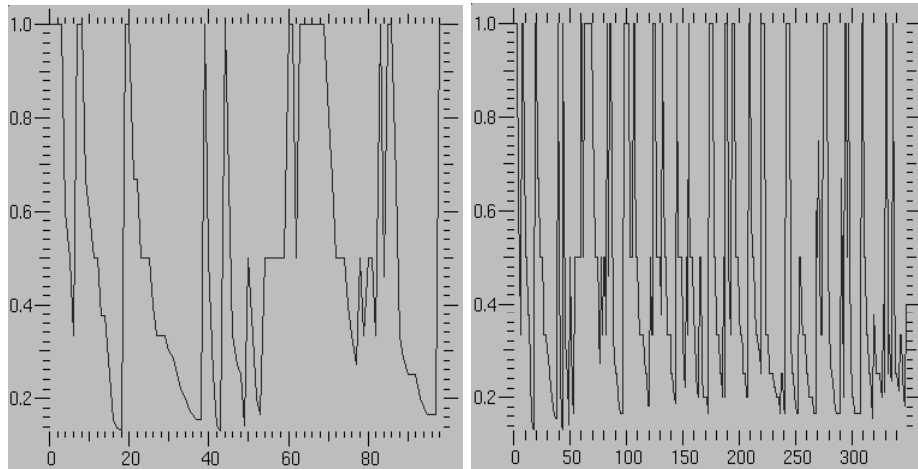


Fig. 2. Priorities of the vertices during the network traversal. The left and the right diagram illustrates the community cutting of 100 and 350 vertices respectively. The initial seed consisted of one vertex in both cases. The highest the priority is, the more neighbours of the vertex has been already assigned to the community.

4 Conclusions and future work

We presented briefly functionalities usually implemented by tools for massive graph analysis. An algorithm for cutting out a part of the graph was proposed. This algorithm is necessary for finding a portion of the graph based on the given initial seed, which can be further processed in the memory.

Further improvement of the algorithm consist in changing the condition for finalisation of the traverse. Setting a minimal threshold of the vertex priority to be processed perhaps yield tighter or wider communities depending on the threshold. As it was shown on fig. 2 the priorities can decrease to low values, signing that the new vertex was surrounded by few vertices already included to the community. We believe that introducing threshold could result better defined community.

We intend to test the approach on theoretical such as random networks or small world model; and real networks, as Web and Wikipedia. We hope that our approach can be useful for finding surrounding topics in Wikipedia and the community including the topic, helping the user navigation. Fig. 3 shows visualised clusters in Wikipedia.

We believe that approaches for finding community only around a seed of vertices, not visiting all vertices of the network are useful for their lower time consumption and applicability on huge networks.

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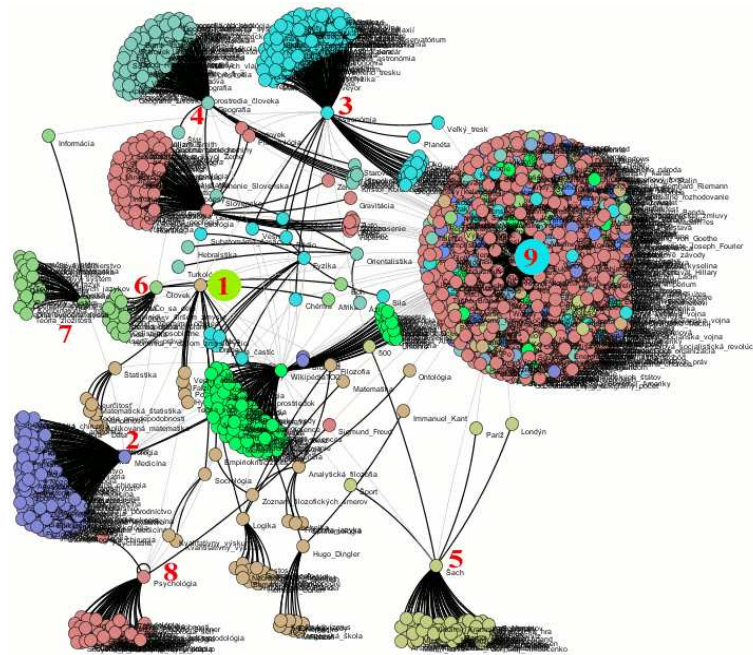


Fig. 3. Visualised part of Slovak Wikipedia. The picture shows that similar topics are referenced by and refers to hub topics such as Medicine (2) or Psychology (8).

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